

# **Cambridge IGCSE**<sup>™</sup>

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### **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/62

Paper 6 Investigation and Modelling (Extended)

February/March 2022

1 hour 40 minutes

You must answer on the question paper.

No additional materials are needed.

#### **INSTRUCTIONS**

- Answer both part A (Questions 1 to 3) and part B (Questions 4 to 8).
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a graphic display calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly, including sketches, to gain full marks for correct methods.
- In this paper you will be awarded marks for providing full reasons, examples and steps in your working to communicate your mathematics clearly and precisely.

#### **INFORMATION**

- The total mark for this paper is 60.
- The number of marks for each question or part question is shown in brackets [ ].

This document has 20 pages. Any blank pages are indicated.

#### Answer both parts A and B.

### A INVESTIGATION (QUESTIONS 1 TO 3)

#### **SEQUENCES OF CENTRED POLYGONS (30 marks)**

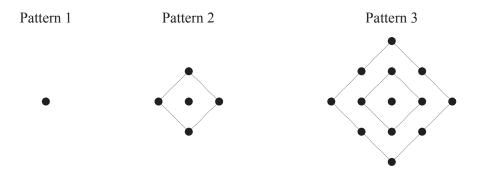
You are advised to spend no more than 50 minutes on this part.

This investigation looks at sequences of centred polygons.

The first pattern in each sequence is a single dot.

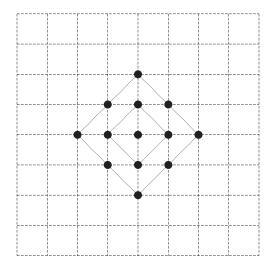
The sequence continues by adding polygons of increasing size around the central dot.

1 (a) Oliver draws this sequence of dot patterns called *centred squares*.



(i) Pattern 3 is drawn on the grid.

Complete the diagram to show Pattern 4.



[1]

(ii) Complete the table.

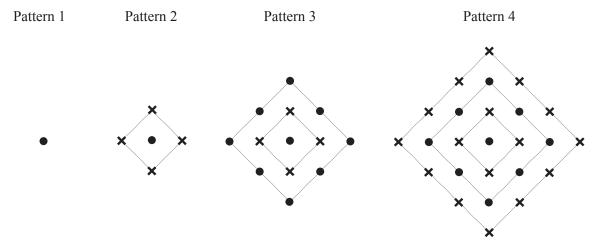
Pattern number, <i>n</i>	1	2	3	4	5
Number of dots	1	5	13		

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(iii) Work out the number of dots in Pattern 7.

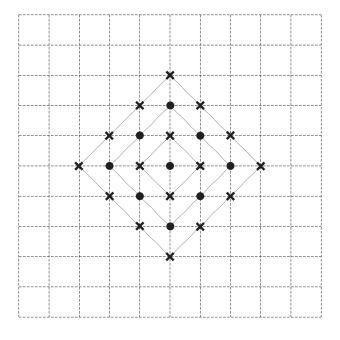
[2
----

**(b)** Oliver draws the dot patterns of centred squares using dots and crosses.



(i) Pattern 4 is drawn on the grid.

Complete the diagram to show Pattern 5.



[1]

## (ii) Complete the table.

Pattern number, <i>n</i>	Number of dots	Number of crosses	Total number of dots and crosses
1	1	0	1
2	1	4	5
3	9	4	13
4		16	
5			
6			

(iii) Complete the table.

Pattern number, <i>n</i>	Number of dots	Number of crosses	Total number of dots and crosses
1	$1 = 1^2$	$0 = 0^2$	$1^2 + 0^2 = 1$
2	$1 = 1^2$	$4 = 2^2$	$2^2 + 1^2 = 5$
3	$9 = 3^2$	$4 = 2^2$	$3^2 + 2^2 = 13$
4		16 =	
5			
6			

[2]

(iv)	Complete the	formula for	the total	number o	of dots	and cro	osses, $T$ ,	in Pattern <i>n</i>	l.
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$$T = \dots$$
 [2]

(v) Show that the formula for T is

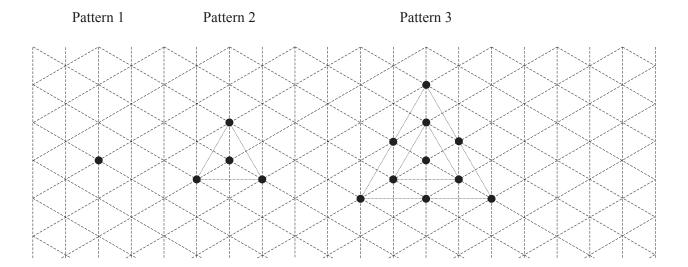
$$2n^2 - 2n + 1$$
.

[1]

(vi) Work out the total number of dots and crosses in Pattern 15.

.....[2]

2 This is the sequence of centred triangles.



(a) Complete the table.

Pattern number, <i>n</i>	1	2	3	4	5
Number of dots, T	1	4	10		

[3]

**(b)** The formula for the number of dots, T, in Pattern n is

$$T = an^2 + bn + c .$$

(i) Give a reason why a is  $\frac{3}{2}$ .

.....[1]

(ii) Find the value of b and the value of c.

*b* = .....

 $c = \dots$  [4]

(c)	There are 571 dots in Pattern $k$ .
	Find the value of $k$ .

$$k =$$
 [4]

3	The formula	a for the number	of dots. T	in the sequ	ence of centred	hexagons is
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$$T = 3n^2 - 3n + 1.$$

The number of dots in the nth centred hexagon is 6 more than the number of dots in the nth centred square.

Find the value of n and the number of dots in the centred hexagon.

	n =	
number of dots in the centred hexas	on :	[3]

#### **B** MODELLING (QUESTIONS 4 TO 8)

#### **DAYLIGHT HOURS** (30 marks)

You are advised to spend no more than 50 minutes on this part.

This task looks at modelling the number of daylight hours throughout the year. The number of daylight hours is the length of time between sunrise and sunset.

4 Sophia looks at the number of daylight hours in London, England.

She knows the shortest number of daylight hours, *shortest day*, is on 21 December. She knows the longest number of daylight hours, *longest day*, is on 21 June.

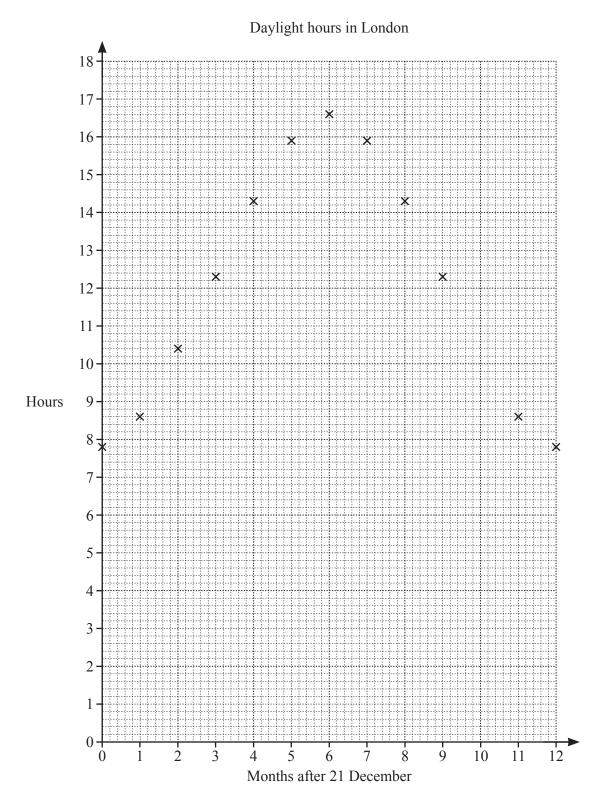
She collects data for the sunrise and sunset times on the 21st day of every month. She works out the length of daylight in hours and minutes and converts it to a time in hours correct to 1 decimal place.

Her results are in this table.

Daylight hours in London								
Month	Day	Sunrise	Sunset	Daylight in hours and minutes	Daylight in hours			
December	21	08 03	1553	7 h 50 min	7.8			
January	21	0752	1630	8 h 38 min	8.6			
February	21	0702	1726	10 h 24 min	10.4			
March	21	0600	1815	12 h 15 min	12.3			
April	21	0551	2007	14h 16 min	14.3			
May	21	05 00	20 54	15 h 54 min	15.9			
June	21	0443	2121	16h 38 min	16.6			
July	21	05 08	21 04	15 h 56 min	15.9			
August	21	05 55	2010	14h 15 min	14.3			
September	21	0645	1900	12h 15 min	12.3			
October	21	0735	1754					
November	21	0728	1603	8 h 35 min	8.6			
December	21	08 03	15 53	7 h 50 min	7.8			

(a) Complete the row for October.

**(b)** Sophia puts her results from the table on this graph.



(i) Plot the value for daylight hours on 21 October.

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[1]

(ii)	Write down the number of daylight hours on the shortest day and on the longest day in London.
	shortest day
	longest day[1]
(:::)	Chart that the length of time helfway between the number of devilight house on the shortest

(iii) Show that the length of time halfway between the number of daylight hours on the shortest day and the number of daylight hours on the longest day is 12.2 hours.

[1]

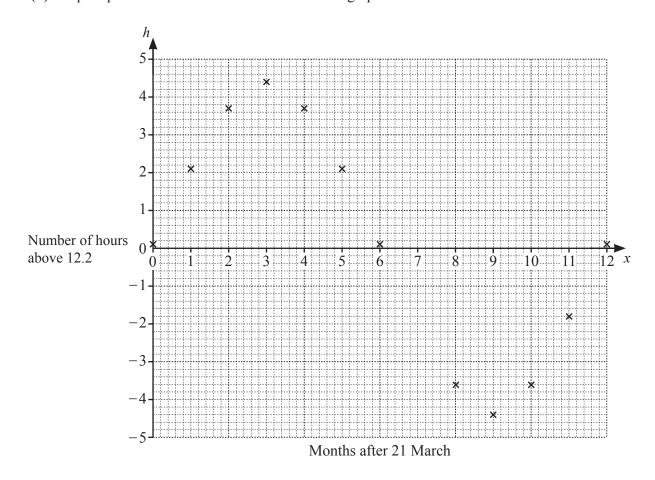
- 5 Sophia changes the order of her table.
  - She starts with 21 March.
  - She works out daylight hours above and below 12.2.

Daylight hours in London						
Month	Day	Sunrise	Sunset	Daylight in hours and minutes	Daylight in hours, H	Daylight in hours above 12.2, h
March	21	0600	1815	12 h 15 min	12.3	0.1
April	21	0551	2007	14h 16min	14.3	2.1
May	21	05 00	20 54	15 h 54 min	15.9	3.7
June	21	0443	2121	16h 38 min	16.6	4.4
July	21	05 08	21 04	15 h 56 min	15.9	3.7
August	21	05 55	2010	14h 15 min	14.3	2.1
September	21	0645	1900	12 h 15 min	12.3	0.1
October	21	0735	1754			
November	21	0728	1603	8 h 35 min	8.6	-3.6
December	21	08 03	15 53	7 h 50 min	7.8	- 4.4
January	21	0752	1630	8 h 38 min	8.6	-3.6
February	21	0702	1726	10 h 24 min	10.4	- 1.8
March	21	0600	1815	12 h 15 min	12.3	0.1

(a) Complete the row for October.

[1]

**(b)** Sophia puts her results from the table into this graph.



Sophia models the number of daylight hours in London using the points on her graph. She decides on this model.

$$h = 4.4\sin(30x)$$

h is the number of daylight hours above 12.2 and x is the number of months after 21 March.

Give a reason why Sophia uses

(i) the number 4.4,

(ii) the number 30.

......

(c)	Sophia changes her model. <i>H</i> is the number of daylight hours and <i>x</i> is the number of months after 21 March.					
	Con	nplete the model for $H$ .				
( <b>1</b> )	40	$H = \dots $ [1]				
(d)	(i)	Use the model in <b>part (c)</b> to calculate the number of daylight hours on 21 April and 21 January.				
		April				
		January[4]				
	(ii)	Sophia thinks that the calculated values for April and January show that her model is a good one.				
		Is she correct? Give a reason for your answer.				
		[1]				
	(iii)	What assumption has Sophia made about the months for her model?				
		[1]				

6 This table shows sunrise and sunset times for Tokyo in Japan on the 21st day of every month.

Sunrise and sunset times in Tokyo				
Month	Day	Sunrise	Sunset	
March	21	0543	1753	
April	21	05 00	1819	
May	21	0432	1844	
June	21	0425	1900	
July	21	0440	1853	
August	21	05 04	1823	
September	21	0528	1739	
October	21	05 52	1658	
November	21	0622	1630	
December	21	0647	1632	
January	21	0648	1656	
February	21	0622	1727	
March	21	0543	1753	

The shortest day is 21 December and the longest day is 21 June.

Find a model for the number of daylight hours, *H*, in Tokyo.

Write your model in the form  $H = A \sin(Bx) + C$ ,

where x is the number of months after 21 March and A, B and C are numbers to be found.

7

This is a model of the number of daylight hours in Cairo in Egypt.
$H = 2\sin(30x) + 12.2$
H is the number of daylight hours and $x$ is the number of months after 21 March.
(a) Use the model to estimate the number of daylight hours on the shortest day in Cairo.
[2]
<b>(b)</b> What is the date of the shortest day in Cairo according to the model?

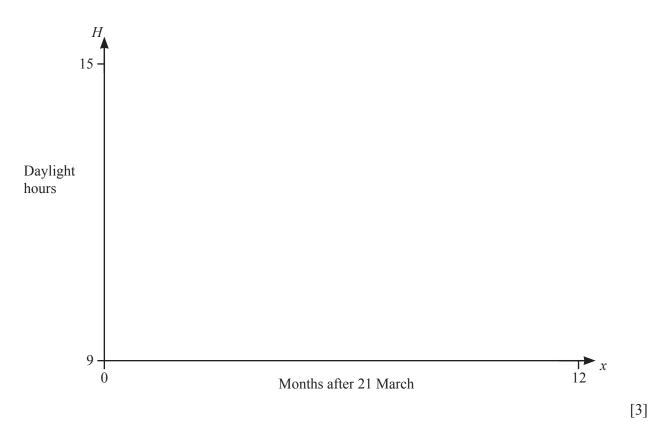
.....[1]

8 This is a model of the number of daylight hours in Melbourne in Australia.

$$H = 2.4 \sin(30x + 180) + 12.2$$

*H* is the number of daylight hours and *x* is the number of months after 21 March.

- (a) On the axes below sketch the models for the number of daylight hours:
  - in Cairo
  - in Melbourne.



(b) Make a statement about the number of daylight hours in Melbourne on the shortest day in Cairo.

[1]

(c) Find the dates when the number of daylight hours in Cairo is the same as it is in Melbourne.

.....[2]

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