

# PROFIT-LOSS-DISCOUNT

- 1** (a) (i) In a camera magazine, 63 pages are used for adverts.  
The ratio number of pages of adverts : number of pages of reviews = 7:5 .

Calculate the number of pages used for reviews.

*Answer(a)(i)* ..... [2]

- (ii) In another copy of the magazine, 56 pages are used for reviews and for photographs.  
The ratio number of pages of reviews : number of pages of photographs = 9:5 .

Calculate the number of pages used for photographs.

*Answer(a)(ii)* ..... [2]

- (iii) One copy of the magazine costs \$4.90 .  
An annual subscription costs \$48.80 for 13 copies.

Calculate the percentage discount by having an annual subscription.

*Answer(a)(iii)* ..... % [3]

- (b) In a car magazine, 25% of the pages are used for selling second-hand cars,  $62\frac{1}{2}\%$  of the **remaining** pages are used for features, and the other 36 pages are used for reviews.

Work out the total number of pages in the magazine.

*Answer(b)* ..... [4]

MARKING SCHEME:

|                |                        |          |  |
|----------------|------------------------|----------|--|
| <b>(a) (i)</b> | 45                     | <b>2</b> | <b>M1</b> for $5 \times 63 \div 7$   |
| <b>(ii)</b>    | 20                     | <b>2</b> | <b>M1</b> for $5 \times 56 \div 14$  |
| <b>(iii)</b>   | 23.4 or 23.38 to 23.41 | <b>3</b> | <p><b>M2</b> for <math>\frac{13 \times 4.9 - 48.8}{13 \times 4.9} \times 100</math><br/> or <math>\frac{4.9 - 48.8 \div 13}{4.9} \times 100</math></p> <p>Or</p> <p><b>M1</b> for <math>\frac{13 \times 4.9 - 48.8}{13 \times 4.9}</math> or <math>\frac{48.8}{13 \times 4.9} \times 100</math> or 76.6[...]</p>   |
| <b>(b)</b>     | 128                    | <b>4</b> | <p>Using fractions (percentages / decimals):</p> <p><b>M1</b> for <math>\frac{3}{4} \times \frac{3}{8} \left[ = \frac{9}{32} \right]</math> or <math>\frac{75}{100} \times 37.5</math> [= 28.125%]</p> <p><b>A1</b> for <math>\frac{9}{32}</math> or 28.125[%]</p> <p><b>M1</b> for <math>36 \div \frac{9}{32}</math> oe</p> <p>or <math>36 \times \frac{100}{28.125}</math> oe</p> <p>Partial percentages</p> <p><b>M1</b> for (Remaining) <math>\frac{100 \times 36}{37.5}</math> [= 96]</p> <p><b>A1</b> for 96</p> <p><b>M1</b> for <math>96 \div \frac{75}{100}</math> oe</p> <p><b>SC1</b> for 288</p> |

**2** (a) In a cycling club, the number of members are in the ratio males : females = 8 : 3.  
The club has 342 females.

(i) Find the total number of members.

..... [2]

(ii) Find the percentage of the total number of members that are female.

..... % [1]

(b) The price of a bicycle is \$1020.  
Club members receive a 15% discount on this price.

Find how much a club member pays for this bicycle.

\$ ..... [2]

(c) In 2019, the membership fee of the cycling club is \$79.50 .  
This is 6% more than last year.

Find the **increase** in the cost of the membership.

\$ ..... [3]

- (d) Asif cycles a distance of 105 km.  
On the first part of his journey he cycles 60 km in 2 hours 24 minutes.  
On the second part of his journey he cycles 45 km at 20 km/h.

Find his average speed for the whole journey.

..... km/h [4]

- (e) Bryan invested \$480 in an account 4 years ago.  
The account pays compound interest at a rate of 2.1% per year.  
Today, he uses some of the money in this account to buy a bicycle costing \$430.

Calculate how much money remains in his account.

\$ ..... [3]

- (f) The formula  $s = \frac{1}{2}at^2$  is used to calculate the distance,  $s$ , travelled by a bicycle.

When  $a = 3$  and  $t = 10$ , each correct to the nearest integer, calculate the lower bound of the distance,  $s$ .

..... [2]

MARKING SCHEME:

|         |                      |   |   |
|---------|----------------------|---|---|
| (a)(i)  | 1254                 | 2 | <b>M1</b> for $342 \div 3$  |
| (a)(ii) | 27.3 or 27.27...     | 1 |   |
| (b)     | 867                  | 2 | <b>M1</b> for $1020 \times \frac{15}{100}$ oe<br>or $1020 \times \left(1 - \frac{15}{100}\right)$ oe  |
| (c)     | 4.5[0]               | 3 | <b>M2</b> for $\frac{79.5[0]}{100+6}[\times 6]$ oe<br>or $\frac{79.5[0]}{100+6} \times 100$ oe<br>or <b>M1</b> for 79.5[0] associated with 106[%]   |
| (d)     | 22.6 or 22.58... nfw | 4 | <b>M1</b> for $\frac{45}{20}$ or better<br>and<br><b>M2</b> for $\frac{60+45}{\text{their } 2\text{h } 24\text{min} + \text{their } \frac{45}{20}}$<br>or <b>M1</b> for $\text{their } \frac{45}{20} + \text{their } 2\text{h } 24\text{min}$ |
| (e)     | 91.6[0] to 91.61     | 3 | <b>M2</b> for $480 \times \left(1 + \frac{2.1}{100}\right)^4 - 430$ oe<br>OR <b>M1</b> for $480 \times \left(1 + \frac{2.1}{100}\right)^4$ oe<br><b>A1</b> for 522, 521.6[0] to 521.61  |
| (f)     | 112.8125             | 2 | <b>B1</b> for 2.5 or 9.5 seen   |

**3**

- (a) Ali and Ben receive a sum of money.  
They share it in the ratio 5 : 1.  
Ali receives \$2345.

Calculate the total amount.

*Answer(a)* \$ ..... [2]

- (b) Ali uses 11% of his \$2345 to buy a television.

Calculate the cost of the television.

*Answer(b)* \$ ..... [2]

- (c) A different television costs \$330.

- (i) Ben buys one in a sale when this cost is reduced by 15%.

How much does Ben pay?

*Answer(c)(i)* \$ ..... [2]

- (ii) \$330 is 12% less than the cost last year.

Calculate the cost last year.

*Answer(c)(ii)* \$ ..... [3]

- (d) Ali invests \$1500 of his share in a bank account.  
The account pays compound interest at a rate of 2.3% per year.

Calculate the total amount in the account at the end of 3 years.

*Answer(d)* \$ ..... [3]

- (e) Ali also buys a computer for \$325.  
He later sells this computer for \$250.

Calculate Ali's percentage loss.

*Answer(e)* ..... % [3]



MARKING SCHEME:

|         |                        |   |  |
|---------|------------------------|---|--|
| (a)     | 2814 final answer      | 2 | <b>M1</b> for $2345 \div 5$ soi by 469 or ans = 2810   |
| (b)     | 257.95 final answer    | 2 | <b>M1</b> for $2345 \times 0.11$ oe or ans = 258   |
| (c) (i) | 280.5[0] final answer  | 2 | <b>M1</b> for $330 \times (1 - 0.15)$ oe or ans = 281  |
| (ii)    | 375                    | 3 | <b>M2</b> for $330 \div (1 - 0.12)$ oe<br>Or <b>M1</b> for $330 = (100 - 12)\%$ oe   |
| (d)     | 1605.89 or 1605.9[0]   | 3 | <b>M2</b> for $1500 \times (1 + 0.023)^3$ oe soi by 1605.898751<br>or $1500 \times 1.07(05\dots)$<br>Or <b>M1</b> for $1500 \times (1 + 0.023)^2$ oe                             |
| (e)     | 23.1 or 23.07 to 23.08 | 3 | <b>M2</b> for $\frac{325 - 250}{325} \times 100$ oe<br>Or <b>M1</b> for $\frac{325 - 250}{325}$ soi by 0.2307... 3sf or better<br>or $\frac{250}{325} \times 100$ soi by 76.9... |

**4**

Anna, Bobby and Carl receive a sum of money.  
They share it in the ratio 12:7:8.  
Anna receives \$504.

**(a)** Calculate the **total** amount.

*Answer(a)* \$ ..... [3]

**(b) (i)** Anna uses 7% of her \$504 to pay a bill.  
Calculate how much she has left.

*Answer(b)(i)* \$ ..... [3]

**(ii)** She buys a coat in a sale for \$64.68.  
This was 23% less than the original price.  
Calculate the original price of the coat.

*Answer(b)(ii)* \$ ..... [3]

**(c)** Bobby uses \$250 of his share to open a bank account.  
This account pays compound interest at a rate of 1.6% per year.  
Calculate the amount in the bank account after 3 years.  
Give your answer correct to 2 decimal places.

*Answer(c)* \$ ..... [3]

**(d)** Carl buys a computer for \$288 and sells it for \$324.  
Calculate his percentage profit.

*Answer(d)* ..... % [3]

MARKING SCHEME:

|                |            |          |   |
|----------------|------------|----------|---|
| <b>(a)</b>     | 1134       | <b>3</b> | <b>M2</b> for $\frac{504}{12} \times (12 + 7 + 8)$ soi by answer of 1130<br>or <b>B1</b> for 27 or 42 or 294 or 336 seen                |
| <b>(b) (i)</b> | 468.72     | <b>3</b> | <b>M2</b> for $\frac{93}{100} \times 504$ oe soi by 468.7 or 469<br>or <b>M1</b> for $\frac{7}{100} \times 504$ (implied by 35.28)      |
| <b>(ii)</b>    | 84         | <b>3</b> | <b>M2</b> for $\frac{64.68}{77} \times 100$<br>or <b>M1</b> for $(100 - 23)\% = 64.68$  |
| <b>(c)</b>     | 262.19 cao | <b>3</b> | <b>M2</b> for $250 \times 1.016^3$ oe implied by answer 262.2<br>or better<br><br>or <b>M1</b> for $250 \times 1.016^n$ oe $n > 2$ seen |
| <b>(d)</b>     | 12.5%      | <b>3</b> | <b>M2</b> for $\frac{324 - 288}{288} \times 100$<br>or <b>M1</b> for $\frac{324}{288} \times 100$ (112.5) or $\frac{36}{288}$ (0.125)   |

- 5** (a) Last year a golf club charged \$1650 for a family membership.  
This year the cost increased by 12%.

Calculate the cost of a family membership this year.

*Answer(a)* \$ ..... [2]

- (b) The golf club runs a competition.  
The total prize money is shared in the ratio 1st prize : 2nd prize = 9 : 5.  
The 1st prize is \$500 more than the 2nd prize.

- (i) Calculate the total prize money for the competition.

*Answer(b)(i)* \$ ..... [2]

- (ii) What percentage of the total prize money is given as the 1st prize?

*Answer(b)(ii)* ..... % [1]

- (c) For the members of the golf club the ratio men : children = 11 : 2.  
The ratio women : children = 10 : 3.

- (i) Find the ratio men : women.

*Answer(c)(i)* ..... : ..... [2]

(ii) The golf club has 24 members who are children.

Find the total number of members.

*Answer(c)(ii)* ..... [3]

(d) The club shop sold a box of golf balls for \$20.40 .  
The shop made a profit of 20% on the cost price.

Calculate the cost price of the golf balls.

*Answer(d)* \$ ..... [3]

MARKING SCHEME:

|         |   |   |   |
|---------|---|---|---|
| (a)     | 1848 final answer                         | 2 | <b>M1</b> for $1650 \times \left(1 + \frac{12}{100}\right)$ oe  |
| (b) (i) | 1750                                      | 2 | <b>M1</b> for $\frac{500}{9-5}$ [ $\times 5$ ] or [ $\times 9$ ] or any equation which would lead to $4x = 500$ or $4x = 2500$ or $4x = 4500$ or $4x = 7000$ when simplified  |
| (ii)    | $64\frac{2}{7}$ or 64.3 or 64.28 to 64.29 | 1 |   |
| (c) (i) | 33 : 20 oe                                | 2 | <b>B1</b> for 33 : 6 or 20 : 6 or 5.5 oe seen or 3.33...oe seen<br>or <b>M1</b> for two ratios with a common number of children implied by $20k$ <b>and</b> $33k$ seen, $k > 0$   |
| (ii)    | 236                                       | 3 | <b>M2</b> for $\frac{24}{2} \times 11 + \frac{24}{3} \times 10$ oe<br>or $((3 \times 11) + (2 \times 10)) \times 24 \div 6$<br>or $\frac{6}{6+20+33} \times x = 24$<br>or <b>M1</b> for $\frac{24}{2} \times 11$ or $\frac{24}{2} \times 13$ soi<br>or $\frac{24}{3} \times 10$ or $\frac{24}{3} \times 13$ soi oe or $24 \div 6$ soi |
| (d)     | 17[.00]                                   | 3 | <b>M2</b> for $20.40 \div \left(1 + \frac{20}{100}\right)$ oe<br>or <b>M1</b> for $(100 + 20)\%$ oe associated with 20.40 seen  |