

## BASIC RULES OF INDICES-SET-1

### WITHOUT FRACTIONAL INDICES

1

- (a) Write down the value of  $x^{-1}$ ,  $x^0$ ,  $x^{\frac{1}{2}}$ , and  $x^2$  when  $x = \frac{1}{4}$ .

*Answer (a)*  $x^{-1} = \dots$

$x^0 = \dots$

$x^{\frac{1}{2}} = \dots$

$x^2 = \dots$  [2]

MS-1

a) 4, 1,  $\frac{1}{2}$ ,  $\frac{1}{16}$  oe isw

B2

allow SC1 for any two correct

2

$$81^x = 3$$

Find the value of  $x$ .

*Answer*  $x = \dots$  [1]

MS-2

$\frac{1}{4}$  or 0.25

1

3

(a)  $3^x = \frac{1}{3}$ .

Write down the value of  $x$ .

*Answer (a)*  $x = \dots$  [1]

(b)  $5^y = k$ .

Find  $5^{y+1}$ , in terms of  $k$ .

*Answer (b)*  $5^{y+1} = \dots$  [1]

|                            |  |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
|----------------------------|--|------------|--------------|---|--|----------------------------|---|----|--------------|------------------|----|---------|--|--|--|
| MS-3                       | <table border="1"> <tr> <td>(a) -1</td><td></td><td>1</td><td></td></tr> <tr> <td>(b) 5k</td><td></td><td>1</td><td></td></tr> </table>  | (a) -1     |              | 1 |  | (b) 5k                     |   | 1  |              |                  |    |         |  |  |  |
| (a) -1                     |  | 1          |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
| (b) 5k                     |  | 1          |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
|                            |  |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
| 4                          | <p>Find the value of <math>n</math> in each of the following statements.</p> <p>(a) <math>32^n = 1</math></p> <p>(b) <math>32^n = 2</math></p> <p>(c) <math>32^n = 8</math></p>  |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
|                            | <p><i>Answer(a)</i> <math>n = \dots</math> [1]</p> <p><i>Answer(b)</i> <math>n = \dots</math> [1]</p> <p><i>Answer(c)</i> <math>n = \dots</math> [1]</p>   |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
|                            |  |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
| MS-4                       | <table border="1"> <tr> <td>(a) 0</td> <td>1</td> <td></td> <td></td> </tr> <tr> <td>(b) 0.2 or <math>1/5</math></td> <td>1</td> <td></td> <td></td> </tr> <tr> <td>(c) 0.6 or <math>3/5</math></td> <td>1✓</td> <td>(b) x 3</td> <td></td> </tr> </table> | (a) 0      | 1            |   |  | (b) 0.2 or $1/5$           | 1 |    |              | (c) 0.6 or $3/5$ | 1✓ | (b) x 3 |  |  |  |
| (a) 0                      | 1  |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
| (b) 0.2 or $1/5$           | 1  |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
| (c) 0.6 or $3/5$           | 1✓   | (b) x 3    |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
|                            |  |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
| 5                          | <p>Find the value of <math>n</math> in the following equations.</p> <p>(a) <math>2^n = 1024</math></p>   |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
|                            | <p><i>Answer(a)</i> <math>n = \dots</math> [1]</p> <p>(b) <math>4^{2n-3} = 16</math></p>   |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
|                            | <p><i>Answer(b)</i> <math>n = \dots</math> [2]</p>   |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
| MS-5                       | <table border="1"> <tr> <td>(a) 10(.0)</td> <td>1</td> <td></td> <td></td> </tr> <tr> <td>(b) <math>2\frac{1}{2}, 2.5(0)</math></td> <td>2</td> <td>M1</td> <td><math>2n - 3 = 2</math></td> </tr> </table>  | (a) 10(.0) | 1            |   |  | (b) $2\frac{1}{2}, 2.5(0)$ | 2 | M1 | $2n - 3 = 2$ |                  |    |         |  |  |  |
| (a) 10(.0)                 | 1  |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |
| (b) $2\frac{1}{2}, 2.5(0)$ | 2  | M1         | $2n - 3 = 2$ |   |  |                            |   |    |              |                  |    |         |  |  |  |
|                            |  |            |              |   |  |                            |   |    |              |                  |    |         |  |  |  |

|   |  |   |   |         |   |                                |  |  |  |
|---|--|---|---|---------|---|--------------------------------|--|--|--|
| <p>6</p> <p><math>a \times 10^7 + b \times 10^6 = c \times 10^6</math></p> <p>Find <math>c</math> in terms of <math>a</math> and <math>b</math>.<br/>Give your answer in its simplest form.</p>   | <p><i>Answer</i> <math>c =</math> ..... [2]</p>    |   |   |         |   |                                |  |  |  |
| <p>MS-6</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 30%; padding: 5px;">10<math>a</math> + <math>b</math> or <math>a \times 10^1 + b (\times 10^0)</math></td> <td style="width: 15%; padding: 5px; text-align: center;">2</td> <td style="width: 55%; padding: 5px;"><b>M1</b> <math>[a \times 10^7 + b \times 10^6] \div 10^6</math></td> </tr> </table>  | 10 $a$ + $b$ or $a \times 10^1 + b (\times 10^0)$  | 2   | <b>M1</b> $[a \times 10^7 + b \times 10^6] \div 10^6$ |         |   |                                |  |  |  |
| 10 $a$ + $b$ or $a \times 10^1 + b (\times 10^0)$   | 2  | <b>M1</b> $[a \times 10^7 + b \times 10^6] \div 10^6$ |   |         |   |                                |  |  |  |
|   |  |   |   |         |   |                                |  |  |  |
| <p>7</p> <p>Find the values of <math>m</math> and <math>n</math>.</p> <p>(a) <math>2^m = 0.125</math></p>   | <p><i>Answer(a)</i> <math>m =</math> ..... [2]</p> |   |   |         |   |                                |  |  |  |
| <p>(b) <math>2^{4n} \times 2^{2n} = 512</math></p>  |  |   |   |         |   |                                |  |  |  |
|   |  |   |   |         |   |                                |  |  |  |
| <p>MS-7</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 30%; padding: 5px;">(a) -3</td> <td style="width: 15%; padding: 5px; text-align: center;">2</td> <td style="width: 55%; padding: 5px;"><b>M1</b> <math>1/2^3</math> or <math>2^{-3}</math></td> </tr> <tr> <td style="width: 30%; padding: 5px;">(b) 1.5</td> <td style="width: 15%; padding: 5px; text-align: center;">2</td> <td style="width: 55%; padding: 5px;"><b>M1</b> <math>2^{6n}</math> or <math>6n = 9</math></td> </tr> </table> | (a) -3   | 2   | <b>M1</b> $1/2^3$ or $2^{-3}$                         | (b) 1.5 | 2 | <b>M1</b> $2^{6n}$ or $6n = 9$ |  |  |  |
| (a) -3  | 2  | <b>M1</b> $1/2^3$ or $2^{-3}$                         |   |         |   |                                |  |  |  |
| (b) 1.5   | 2  | <b>M1</b> $2^{6n}$ or $6n = 9$                        |   |         |   |                                |  |  |  |
|   |  |   |   |         |   |                                |  |  |  |

8

(a)  $\left(\frac{3}{8}\right)^{\frac{3}{8}} \times \left(\frac{3}{8}\right)^{\frac{1}{8}} = p^q$

Find the value of  $p$  and the value of  $q$ .

Answer(a)  $p = \dots$

$q = \dots$  [2]

(b)  $5^{-3} + 5^{-4} = k \times 5^{-4}$

Find the value of  $k$ .

Answer(b)  $k = \dots$  [2]

MS-8

(a)  $p = \frac{3}{8}$   $q = \frac{1}{2}$

(b)  $k = 6$

2

2

**B2**  $p = \frac{9}{64}$  and  $q = \frac{1}{4}$  or **B1**  $p = \frac{3}{8}$   $q \neq \frac{1}{2}$

**M1** for a correct statement for  $k$  e.g.  $\frac{5^{-3}+5^{-4}}{5^{-4}}$  or for the factorisation  $5^{-4}(5+1) = k \times 5^{-4}$  or  $\frac{1}{625}(5+1) = \frac{k}{625}$

9

Work out.  
 $2^{-4} \times 2^5$

$\dots$  [1]

MS-9

2

1

|       |  |     |   |   |  |     |                         |   |   |
|-------|--|-----|---|---|--|-----|-------------------------|---|---|
| 10    | <p>Simplify.</p> <p>(a) <math>(m^5)^2</math></p> <p>..... [1]</p> <p>(b) <math>4x^3y \times 5x^2y</math></p> <p>..... [2]</p>  |     |   |   |  |     |                         |   |   |
| MS-10 | <table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 15%;">(a)</td><td><math>m^{10}</math> final answer</td><td style="width: 15%;">1</td><td></td></tr> <tr> <td>(b)</td><td><math>20x^5y^2</math> final answer</td><td>2</td><td><b>B1</b> for 2 out of 3 elements correct in final answer or correct answer spoiled</td></tr> </table> | (a) | $m^{10}$ final answer   | 1 |  | (b) | $20x^5y^2$ final answer | 2 | <b>B1</b> for 2 out of 3 elements correct in final answer or correct answer spoiled |
| (a)   | $m^{10}$ final answer  | 1   |   |   |  |     |                         |   |   |
| (b)   | $20x^5y^2$ final answer  | 2   | <b>B1</b> for 2 out of 3 elements correct in final answer or correct answer spoiled |   |  |     |                         |   |   |
| 11    | <p>(a) <math>t^x \times t^2 = t^{10}</math></p> <p>Find the value of <math>x</math>.</p> <p><math>x = \dots</math> [1]</p> <p>(b) Simplify.</p> <p>(i) <math>\left(\frac{4}{x}\right)^{-2}</math></p> <p>..... [1]</p> <p>(ii) <math>a^3b^7 \div a^6b^2</math></p> <p>..... [2]</p>  |     |   |   |  |     |                         |   |   |

|       |         |   |   |  |
|-------|---------|---|---|--|
| MS-11 | (a)     | 8   | 1 |  |
|       | (b)(i)  | $\frac{x^2}{16}$ final answer                 | 1 |  |
|       | (b)(ii) | $a^{-3}b^5$ or $\frac{b^5}{a^3}$ final answer | 2 | <b>B1</b> for $a^{-3}b^k$ or $a^k b^5$ |
|       |         |   |   |  |
|       |         |   |   |  |