



# **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

### **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/42

Paper 4 (Extended)

October/November 2014

2 hours 15 minutes

Candidates answer on the Question Paper.

Additional Materials: Geometrical Instruments

**Graphics Calculator** 

#### **READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

Do not use staples, paper clips, glue or correction fluid.

You may use an HB pencil for any diagrams or graphs.

DO NOT WRITE IN ANY BARCODES.

## Answer all the questions.

Unless instructed otherwise, give your answers exactly or correct to three significant figures as appropriate. Answers in degrees should be given to one decimal place.

For  $\pi$ , use your calculator value.

You must show all the relevant working to gain full marks and you will be given marks for correct methods, including sketches, even if your answer is incorrect.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 120.



# Formula List

For the equation  $ax^2 + bx + c = 0$ 

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Curved surface area, A, of cylinder of radius r, height h.

$$A = 2\pi rh$$

Curved surface area, A, of cone of radius r, sloping edge l.

$$A = \pi r l$$

Curved surface area, A, of sphere of radius r.

$$A = 4\pi r^2$$

Volume, V, of pyramid, base area A, height h.

$$V = \frac{1}{3}Ah$$

Volume, V, of cylinder of radius r, height h.

$$V = \pi r^2 h$$

Volume, V, of cone of radius r, height h.

$$V = \frac{1}{3}\pi r^2 h$$

Volume, V, of sphere of radius r.

$$V = \frac{4}{3}\pi r^3$$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Area = 
$$\frac{1}{2}bc \sin A$$

$$c$$
 $b$ 
 $a$ 
 $C$ 

# Answer all the questions.

1

(a)	Asha and Karim share a sum of money in the ratio Asha: Karim = 5:4. Asha receives \$600.	
	Show that Karim receives \$480.	
		[1]
<b>(b)</b>	Asha spends 20% of her \$600 and invests the remaining money at a rate of 4% per year simple interest.	
	Calculate the amount Asha has at the end of 3 years.	
	Answer(b) \$	[4]
(c)	Karim invests all of his \$480 at a rate of 3.5% per year compound interest.	
	(i) Calculate the amount Karim has at the end of 3 years.	
	Answer(c)(i) \$	[3]
	(ii) Calculate the minimum number of whole years it takes for Karim's \$480 to double in value.	
	Answer(c)(ii)	[3]

2	The	A train leaves Beijing at 15 52 and takes 13 hours and 45 minutes to reach Xian. The distance from Beijing to Xian is 1200 km. The cost of a ticket is 441 Yuan (¥).											
	(a)	Calculate the cost per kilometre to travel	from Beijing	g to Xian.									
	(b)	Find the time that the train arrives in Xiai		¥	[1]								
			Answer(b)		[1]								
	(c)	Calculate the average speed of the train.											
			Answer(c)	km/h	[2]								
	(d)	One day the train is delayed and arrives in	n Xian at 05	58.									
		For this train, calculate the percentage inc	crease on the	e scheduled journey time of 13 h 45 min.									
			Answer(d)	%	[4]								
	(e)	The ticket price of ¥441 is a 5% increase	on the previ	ous price of a ticket.									
		Calculate the previous price of a ticket.											
			Answer(e)	¥	[3]								

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П	I =	130	etud	lents}
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 $T = \{\text{students}\}\$ 

 $C = \{\text{students who go to the cinema}\}\$ 

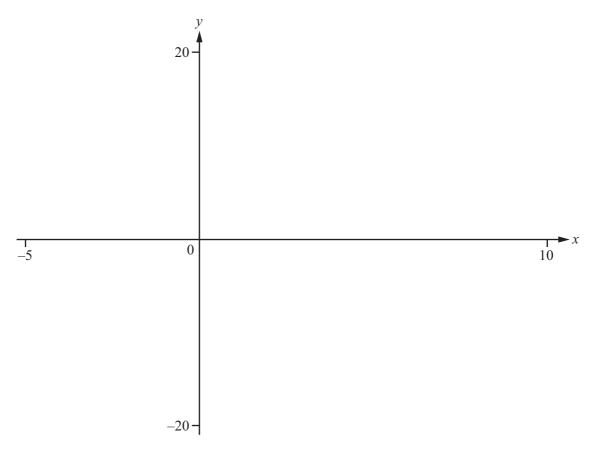
(:	a)	(i)	How many	z students g	o to	the theatre	but do	not go to	o the	cinema'
16	<i>a j</i>	(1)	110 w many	students g	o w	me meane	out uo	not go u	Juic	Cilicilia :

(c) Two of the students who go to the theatre are chosen at random.

Find the probability that they both also go to the cinema.

		Answer(a)(i)		[1]				
	(ii) Find $n(T \cup C)$ .							
		Answer(a)(ii)		[1]				
	(iii) Find $n(T' \cup C)$ .							
		Answer(a)(iii)		[1]				
<b>(b)</b>	One of the 30 students is chosen at random.							
	Find the probability that this stude	ent						
	(i) goes to the cinema,							
		Answer(b)(i)		[1]				
	(ii) either goes to the theatre or o	does not go to the cinema	1.					
		Answer(b)(ii)		[1]				

Answer(c) [3]



$$f(x) = \frac{x^2}{(x-2)}, x \neq 2$$

(a) On the diagram, sketch the graph of y = f(x), for values of x between -5 and 10. [2]

**(b)** Find the co-ordinates of

(i) the local maximum point,

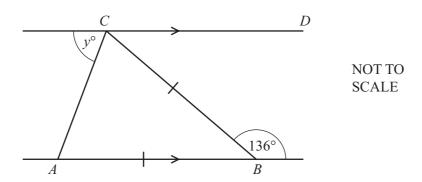
Answer(b)(i) ( \_\_\_\_\_\_ , \_\_\_\_\_ ) [1]

(ii) the local minimum point.

Answer(b)(ii) ( , , , , ) [1]

(c)	Wri	te down the range of $f(x)$ for $x \in \mathbb{R}$ .	
(d)	Wri	te down an integer value of $k$ for which the equation $f(x) = k$ has no solutions.	[2]
(e)	Wri	te down the equation of the vertical asymptote of the graph of $y = f(x)$ .	[1]
		Answer(e)	[1]
<b>(f)</b>	(i)	On the same diagram, sketch the graph of $y = x + 2$ .	[1]
	(ii)	Complete the following statement.	
		The graph of $y = x + 2$ is of the graph of $y = f(x)$ .	[1]
(g)		$g(x) = 1.5^x + 10$	
	(i)	On the same diagram, sketch the graph of $y = g(x)$ .	[2]
	(ii)	Solve the inequality $g(x) < f(x)$ .	
		Answer(g)(ii)	[2]

5 (a)

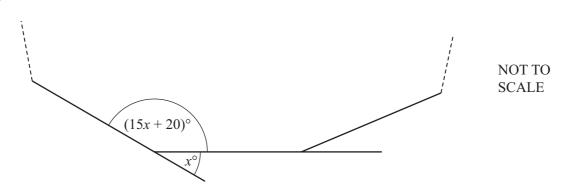


In the diagram, CD and AB are parallel and AB = BC.

Find the value of *y*.

Answer(a) y = [3]

**(b)** 



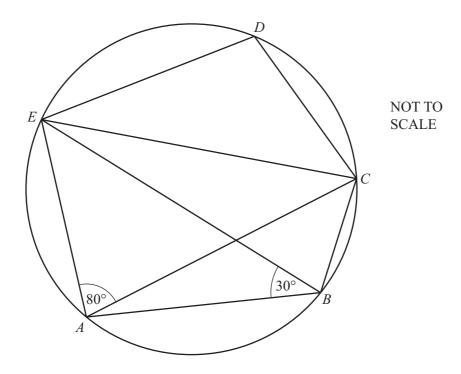
The diagram shows part of a regular polygon.

The interior angle is  $(15x + 20)^{\circ}$  and the exterior angle is  $x^{\circ}$ .

Find the number of sides of this polygon.

Answer(b) [4]

(c)



The points A, B, C, D and E lie on the circumference of a circle.

Find

(i) angle ACE,

$$Answer(c)(i)$$
 Angle  $ACE =$  [1]

(ii) angle AEC,

$$Answer(c)(ii) Angle AEC =$$
 [1]

(iii) angle EDC.

**6** (a) The time taken, t minutes, for each of 100 cars to complete the same journey is recorded.

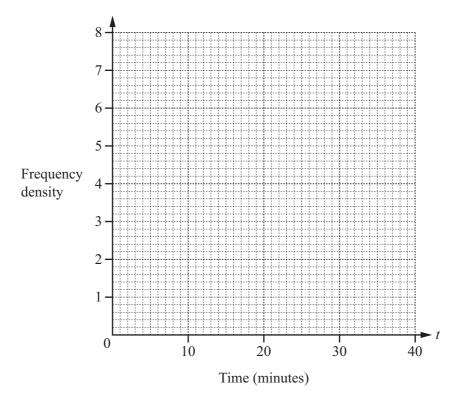
Time (t minutes)	$0 < t \le 10$	$10 < t \le 15$	$15 < t \le 20$	$20 < t \le 40$
Frequency	4	38	34	24

(i) Calculate an estimate of the mean.

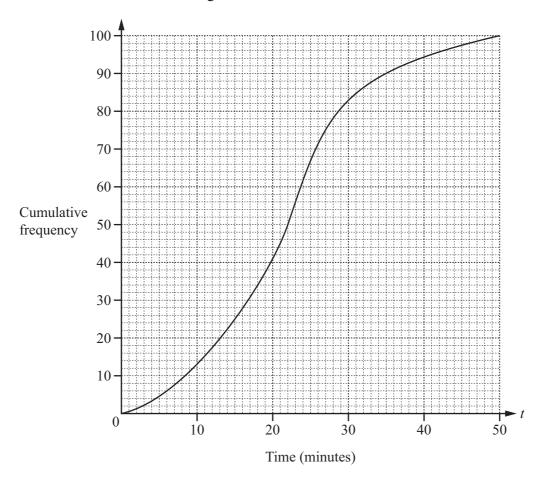
$$Answer(a)(i)$$
 min [2]

[3]

(ii) On the grid, draw a histogram to show the information given in the table.



**(b)** The time taken, *t* minutes, for each of another 100 cars to complete the same journey is recorded. The information is shown in the diagram below.



Find

(i) the median,

Answer(b)(i) min [1]

(ii) the inter-quartile range,

Answer(b)(ii) min [2]

(iii) the number of cars taking more than 35 minutes.

Answer(b)(iii) [2]

7	(a)	Solve the simultaneous equations.
		Show your working.

$$x + 2y = 4$$
$$2x + 5y = 11$$

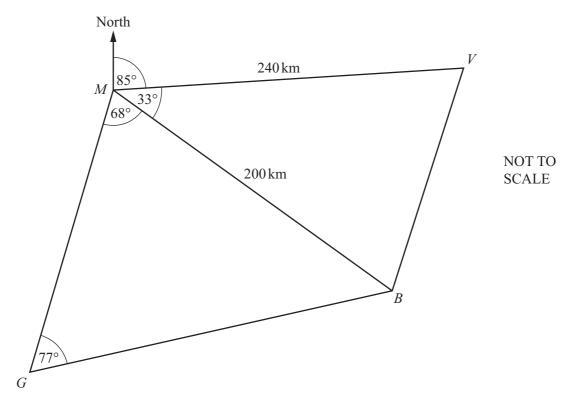
Answer(a)	x =	
	v =	[3]

**(b)** Solve the equation to find x in terms of k.

$$\frac{x+2}{7} - \frac{2x-1}{3} = k$$

$$Answer(b) \quad x =$$
 [4]

(c)	Nev	brary spends \$120 on newspapers and \$90 on magazines. wspapers cost $x$ each. gazines cost $x$ each.				
	(i)	Write down, in terms of $x$ , the number of newspapers that can be bought for \$120.				
		Answer(c)(i)	[1]			
	(ii)	Write down, in terms of $x$ , the number of magazines that can be bought for \$90.				
		Answer(c)(ii)	[1]			
	(iii)	The <b>total</b> number of newspapers and magazines that the library buys is 225.				
		Find the cost of a newspaper.				
		Answer(c)(iii) \$	[4]			



The diagram shows the straight line distances between Milan (M), Venice (V), Bologna (B) and Genoa (G).

(a) Calculate the distance BV.

Answer(a) km [3]

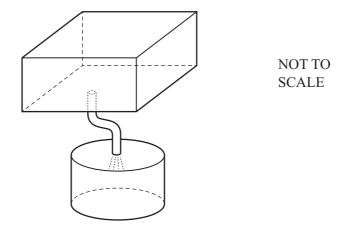
**(b)** Calculate the distance *GB*.

Answer(b) km [3]

(c) A map of the region is drawn to a scale of 1:1000000.

	Answer(c) cm <sup>2</sup>
	Answer(c) cm <sup>2</sup>
The bearing of $V$ from $M$ is $085^{\circ}$ .	
Calculate the bearing of	
(i) $G$ from $M$ ,	
	Answer(d)(i)
(ii) $M$ from $V$ .	
	Answer(d)(ii)

9 The diagram shows two containers, a cuboid and a cylinder, connected by a pipe.

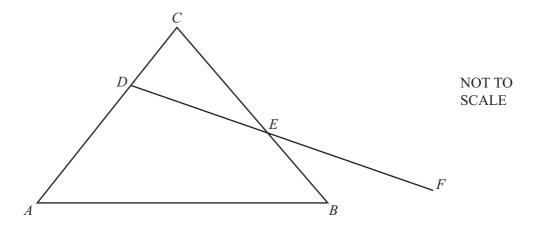


The cuboid measures 1.5 m by 1.5 m by 1 m. It is filled with water. The cylinder is empty. It has radius 80 cm and height 90 cm.

Water flows from the cuboid to the cylinder until the cylinder is full. The water flows through the pipe at a rate of 35 cm<sup>3</sup> per second.

(a) Calculate the time taken to fill the cylinder.
Give your answer in hours and minutes, correct to the nearest minute.

	Answ	er(a)	 h	 min	[5]
(b)	Calculate the amount of water remaining in the Give your answer in cm <sup>3</sup> , correct to 2 significant				
	Answ	er(b)		cm <sup>3</sup>	[4]
(c)	Write your answer to <b>part (b)</b> in standard form.				
	Answ	er(c)	 	 cm <sup>3</sup>	[1]



In the diagram AD = 2DC,  $BE = \frac{1}{2}EC$  and DEF is a straight line.

$$\overrightarrow{AB} = \mathbf{r} \text{ and } \overrightarrow{BC} = \mathbf{t}.$$

- (a) Find, in terms of r and t, in their simplest forms,
  - (i)  $\overrightarrow{AC}$ ,

Answer(a)(i)	Γ1	7	ı

(ii)  $\overrightarrow{DE}$ .

**(b)**  $\overrightarrow{EF} = \frac{1}{3} \mathbf{r} - \frac{1}{3} \mathbf{t}$ .

(i) Find  $\overrightarrow{BF}$  in terms of **r** and/or **t**.

$$Answer(b)(i)$$
 [1]

(ii) What does your answer show about the point F?

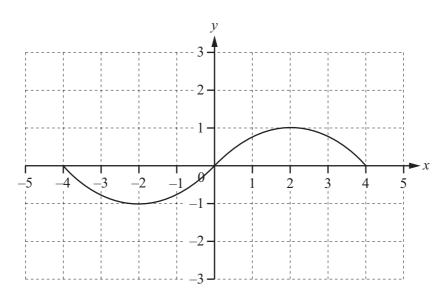
[1]

**11** (a) f(x) = 2x + 1

Find f(f(2)).

Answer(a) [2]

**(b)** 



The diagram shows the graph of y = g(x).

- (i) On the same diagram, sketch the graph of y = g(x + 1). [2]
- (ii) Describe fully the **single** transformation that maps the graph of y = g(x) onto the graph of y = g(x + 1).

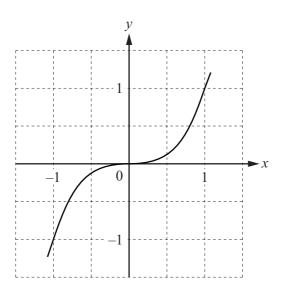
[2]

(c)  $h(x) = x^3$ 

(i) Find  $h^{-1}(x)$ .

Answer(c)(i) [1]

(ii)

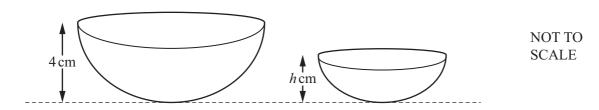


The diagram shows the graph of y = h(x).

(a) On the same diagram, sketch the graph of  $y = h^{-1}(x)$ . [1]

**(b)** Describe fully the **single** transformation that maps the graph of y = h(x) onto the graph of  $y = h^{-1}(x)$ .

[2]



The two bowls are mathematically similar.

The table shows some information about these bowls.

Bowl	Height (cm)	Surface area (cm <sup>2</sup> )	Volume (cm <sup>3</sup> )
Large bowl	4	A	500
Small bowl	h	90	108

Cal	cul	late
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Answer(a)		cm	[3	
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**(b)** the surface area of the large bowl,  $A \text{ cm}^2$ .

Answer(b)  $cm^2$  [2]

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