

# **Cambridge Assessment International Education**

Cambridge International General Certificate of Secondary Education

#### **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/42

Paper 4 (Extended)

October/November 2017

MARK SCHEME
Maximum Mark: 120

## **Published**

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## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

# Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

### **Abbreviations**

awrt answers which round to cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working nfww not from wrong working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

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| Question  | Answer                                                     | Marks | Partial Marks                                                                                                   |
|-----------|------------------------------------------------------------|-------|-----------------------------------------------------------------------------------------------------------------|
| 1(a)(i)   | - 1<br>- 8                                                 | 2     | B1 for each                                                                                                     |
| 1(a)(ii)  | -7n + 34 oe final answer                                   | 2     | <b>B1</b> for $-7n + k$ or $-kn + 34$ oe or correct unsimplified seen                                           |
| 1(b)(i)   | 128, 256                                                   | 2     | B1 for each                                                                                                     |
| 1(b)(ii)  | $2^{n+2}$ oe final answer nfww                             | 2     | M1 for $k \times 2^p (k \neq 0)$ seen, $k$ numerical and $p = f(n)$                                             |
| 2(a)(i)   | 55.25                                                      | 2     | <b>M1</b> for $65 \times 0.85$ oe                                                                               |
| 2(a)(ii)  | $\frac{99}{320}$ cao                                       | 2     | <b>B1</b> for 80 or <b>M1</b> for 24.75 + <i>their</i> 55.25                                                    |
| 2(b)      | 95[.00]                                                    | 3     | M2 for 80.75 ÷ 0.85 oe<br>or M1 for recognising 80.75 as 85%.                                                   |
| 2(c)      | 23.5                                                       | 2     | M1 for $0.85 \times 0.90$ oe or $\frac{0.9 \times their(a)(i)}{65}$ oe 0.765 implies M1                         |
| 3(a)(i)   | Image at (2, 4), (3, 6), (6, 6), (6, 4)                    | 2     | SC1 for reflection in other horizontal line or in the line $x = 1$                                              |
| 3(a)(ii)  | Image at $(-4, -2)$ , $(-6, -3)$ , $(-6, -6)$ , $(-4, -6)$ | 2     | SC1 for correct orientation but wrong centre                                                                    |
| 3(a)(iii) | Reflection $y = -x$ oe                                     | 2     | B1 for each                                                                                                     |
| 3(b)      | Enlargement [centre] (0, 0) oe [factor] - 0.5 oe           | 3     | B1 for each                                                                                                     |
| 3(c)      | Image at $(2, -4)$ , $(6, -4)$ , $(6, -8)$ , $(3, -8)$     | 2     | SC1 for stretch with x-axis invariant with other factor or stretch with $y = k$ invariant with stretch factor 2 |
| 4(a)      | Correct sketch                                             | 3     | B1 for correct middle branch B1 for correct left hand branch B1 for correct right hand branch                   |

© UCLES 2017 Page 3 of 7

| Question     | Answer                                                      | Marks | Partial Marks                                                                                                                                                          |
|--------------|-------------------------------------------------------------|-------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 4(b)         | - 1<br>2                                                    | 2     | B1 for each                                                                                                                                                            |
| 4(c)         | 2                                                           | 1     |                                                                                                                                                                        |
| 4(d)(i)      | Correct sketch                                              | 2     | Must intersect <i>y</i> -axis and be above <i>x</i> -axis <b>B1</b> for decreasing exponential graph                                                                   |
| 4(d)(ii)     | y = 1 oe                                                    | 1     |                                                                                                                                                                        |
| 4(e)         | - 0.892 or - 0.8919 to - 0.892[0]<br>2.62 or 2.622 to 2.623 | 2     | B1 for each                                                                                                                                                            |
| 5(a)         | 22 100                                                      | 4     | <b>B3</b> for 22 140 or 22 143 seen and incorrectly or not rounded or <b>M2</b> for 17 $500 \times 1.04^6$ oe or <b>M1</b> for 17 $500 \times 1.04^k$ $k > 1$ oe       |
| 5(b)         | 1.5[0] or 1.499 to 1.5[00]                                  | 3     | M2 for $\sqrt[12]{\frac{239.12}{200}}$<br>or M1 for $200 \times x^{12} = 239.12$ or better                                                                             |
| 6(a)(i)      | 50 < <i>t</i> ≤ 60                                          | 1     |                                                                                                                                                                        |
| 6(a)(ii)     | Correct curve                                               | 4     | B2 for 3 or 4 correct heights or B1 for 2 correct heights or correct cumulative frequencies seen B1 for plotting correct t co-ordinates, dependent on increasing curve |
| 6(a)(iii)(a) | 52 to 55                                                    | 1     | FT their curve, dependent on increasing                                                                                                                                |
| 6(a)(iii)(b) | Strict follow through                                       | 2     | FT their curve, dependent on increasing B1FT for their cum freq value soi                                                                                              |
| 6(b)(i)      | 52.5 or 52.48 to 52.49                                      | 2     | M1 for evidence of at least three correct mid-values 30, 45, 52.5, 57.5, 70 soi by 10497.5                                                                             |
| 6(b)(ii)     | 1.3,, 11, 8.4, 1.9                                          | 2     | B1 for 3 correct                                                                                                                                                       |
| 6(b)(iii)    | Correct histogram                                           | 3     | FT their (ii) B1 for correct widths B2 for correct heights or B1 for three correct heights                                                                             |

© UCLES 2017 Page 4 of 7

# Cambridge IGCSE – Mark Scheme **PUBLISHED**

| Question  | Answer                                                       | Marks | Partial Marks                                                                                                                 |
|-----------|--------------------------------------------------------------|-------|-------------------------------------------------------------------------------------------------------------------------------|
| 7(a)      | $x + 2\left(x + \frac{1}{4}\right) = 8  \text{oe}$           | M2    | M1 for $2\left(x+\frac{1}{4}\right)$ oe seen                                                                                  |
|           | 2.5                                                          | B1    |                                                                                                                               |
| 7(b)(i)   | $x^3 = 2x(x-2)(x-2)$ oe                                      | M1    |                                                                                                                               |
|           | $[(x-2)^2 =] x^2 - 2x - 2x + 4$ or $2x^3 - 4x^2 - 4x^2 + 8x$ | B1    | Allow $-4x$ for $-2x - 2x$<br>Allow $-8x^2$ for $-4x^2 - 4x^2$                                                                |
|           | leading to $x^3 - 8x^2 + 8x = 0$                             | A1    | Final equation reached without any errors or omissions                                                                        |
| 7(b)(ii)  | Correct sketch                                               | 2     | B1 for correct shaped cubic with max before min                                                                               |
| 7(b)(iii) | 318 or 319 or 318.3 to 318.7                                 | 2     | <b>B1</b> for 6.83 or 6.828 seen isw use of other values (1.1715)                                                             |
| 8(a)(i)   | $\frac{2}{6}$ oe                                             | 1     |                                                                                                                               |
| 8(a)(ii)  | $\frac{4}{6}$ oe                                             | 1     |                                                                                                                               |
| 8(a)(iii) | $\frac{4}{6}$ oe                                             | 1     |                                                                                                                               |
| 8(b)(i)   | $\frac{1}{36}$ oe                                            | 2     | <b>M1</b> for $\frac{1}{6} \times \frac{1}{6}$                                                                                |
| 8(b)(ii)  | $\frac{4}{36}$ oe                                            | 3     | M2 for $\frac{1}{6} \times \frac{2}{6} + \frac{2}{6} \times \frac{1}{6}$ oe<br>or M1 for one product soi by $\frac{1}{18}$ oe |
| 8(c)      | $\frac{215}{216}$ oe                                         | 2     | <b>M1</b> for $1 - \frac{1}{6} \times \frac{1}{6} \times \frac{1}{6}$ oe                                                      |

| Question  | Answer                                         | Marks | Partial Marks                                                                                                                                                                                                                                                                                                                                                                                                  |
|-----------|------------------------------------------------|-------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 9(a)(ii)  | $[y=] 5x-3$ $y = -\frac{1}{5}x + 2 \text{ oe}$ | 2     | M1 for gradient = $\frac{12-2}{3-1}$ oe  M1 for substituting (1, 2) or (3, 12) into $y = mx + c$ OR  M2 for $\frac{y-2}{x-1} = \frac{12-2}{3-1}$ oe  FT their gradient in (i)  M1 for answer in form $y = mx + 2$ oe or for $y = \frac{-1}{their} x + c$ oe                                                                                                                                                    |
| 9(b)(i)   | $-2, \frac{2}{3}$ oe with correct working      | 3     | B2 for sketch with one –ve and one +ve zero or B1 for sketch of parabola vertex downwards  OR B2 for $(3x-2)(x+2)$ or B1 for $3x(x+2)-2(x+2)$ or $x(3x-2)+2(3x-2)$ or for $(3x+a)(x+b)$ where $ab = -4$ or $a + 3b = 4$ OR B2 for $\frac{-4 \pm \sqrt{4^2 - 4(3)(-4)}}{2(3)}$ oe or B1 for $\sqrt{4^2 - 4(3)(-4)}$ or $\frac{-4 \pm \sqrt{\dots}}{2(3)}$ If 0 or B1 scored, then + B1 for $-2$ , $\frac{2}{3}$ |
| 9(b)(ii)  | $-2 < x < \frac{2}{3}$                         | 2     | FT their (b)(i)  B1 for $-2 < x$ or for $x < \frac{2}{3}$ seen  If 0 scored SC1 FT for $-2 \le x \le \frac{2}{3}$                                                                                                                                                                                                                                                                                              |
| 9(c)      | [a =] -4, [b =] 8, [c =] 1                     | 3     | M2 for $y = a(x-1)^2 + 5$<br>or M1 for use of $y = a(x-h)^2 + k$ or<br>for $c = 1$ or $-\frac{b}{2a} = 1$                                                                                                                                                                                                                                                                                                      |
| 10(a)(i)  | 125                                            | 1     |                                                                                                                                                                                                                                                                                                                                                                                                                |
| 10(a)(ii) | 305                                            | 2     | FT their (i), Dep on (i) < 180<br>M1 for 180 + their(i), Dep on (i) < 180                                                                                                                                                                                                                                                                                                                                      |

| Question  | Answer                                              | Marks | Partial Marks                                                                                                                                                            |
|-----------|-----------------------------------------------------|-------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 10(b)     | 69.3 or 69.32 to 69.33                              | 3     | M1 for $90^2 + 120^2 - 2 \times 90 \times 120 \cos 35$<br>A1 for 4806                                                                                                    |
| 10(c)     | 60.3 or 60.28 to 60.29                              | 3     | M2 for $\frac{115 \sin 65}{120}$ oe<br>or M1 for $\frac{115}{\sin BAC} = \frac{120}{\sin 65}$ oe                                                                         |
| 10(d)(i)  | 8730 or 8728 to 8730                                | 4     | M1 for $0.5 \times 90 \times 120 \times \sin 35$<br>M2 for $0.5 \times 120 \times 115 \times \sin(180 - 65 - their (c))$ oe or M1 for angle $ACB = 180 - 65 - their (c)$ |
| 10(d)(ii) | 349 or 349.1 to 349.2                               | 3     | FT their (d)(i) ÷ 25<br>M2 for their (i) ÷ 25 oe<br>or M1 for squaring scale oe<br>or for figs 349 or 3491 to 3492                                                       |
| 11(a)(i)  | 10                                                  | 1     |                                                                                                                                                                          |
| 11(a)(ii) | 1                                                   | 1     |                                                                                                                                                                          |
| 11(b)     | $\frac{x-1}{2}$ oe                                  | 2     | M1 for $y - 1 = 2x$ or $x = 2y + 1$ or $\frac{y}{2} = x + \frac{1}{2}$                                                                                                   |
| 11(c)     | $4x^2 + 4x + 2$ final answer                        | 3     | M1 for $(2x+1)^2 + 1$<br>B1 for $[(2x+1)^2 =] 4x^2 + 2x + 2x + 1$ oe                                                                                                     |
| 11(d)     | Translation $\begin{pmatrix} 0 \\ -2 \end{pmatrix}$ | 2     | B1 for each                                                                                                                                                              |
| 11(e)     | 3                                                   | 1     |                                                                                                                                                                          |